# Multi-color photometric investigation of the totally eclipsing binary NO Camelopardalis 

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#### Abstract

Multi-color photometric light curves of NO Camelopardalis in $V, R_{C}$, and $I_{C}$ bands are obtained and analyzed simultaneously using the Wilson-Devinney program. The solutions suggest that NO Cam is an A-subtype overcontact binary with a mass ratio of $q=0.439$ and a contact degree of $f=55.5 \%$. The small temperature difference ( $\Delta T=44 \mathrm{~K}$ ) between its two components indicates that the system is under thermal contact. The high orbital inclination ( $i=84.5$ ) strengthens our confidence in the parameters determined from the light curves. All available times of minimum light are collected and period variations are analyzed for the first time. The $O-C$ curve reveals that its period is increasing continuously at a rate of $d P / d t=+1.46 \times 10^{-9}$, which can be explained by mass transfer from the less massive component to the more massive one. After the upward parabolic variation is subtracted, the residuals suggest that there may be a cyclic variation with a period of 2.23 yr and an amplitude of $A_{3}=0.00153 \mathrm{~d}$, which may due to the light-traveltime effect arising from the gravitational influence of a close-in tertiary component. The close-in companion reveals that early dynamic interaction among a triple system may have played a very important role in the formation of the W UMa-type binaries.


Key words: binaries: close - binaries: eclipsing — stars: individual (NO Camelopardalis)

## 1 Introduction

The formation and evolutionary theory of W UMa-type binaries is still an open issue. The most widely held view is that they are formed from initially detached binaries through nuclear evolution and angular momentum loss in the pre-contact phase. They will ultimately coalesce into single rapidly rotating stars, which may be progenitors of
the poorly understood blue stragglers, FK Com-type stars, fast rotating A or F dwarf stars, and so on (Bradstreet \& Guinan 1994). It has been demonstrated that the eruption of V1309 Sco was the result of a cool overcontact binary's merger (Nandez et al. 2014). Binnendijk (1970) divided the W UMa-type binaries into A and W subtypes. For A-subtype systems, the more massive component is the

Table 1. Coordinates of NO Cam, UCAC4 827-007726, and UCAC4 827-007718.

| Targets | Name | $\alpha_{\mathrm{J} 2000.0}$ | $\delta_{\mathrm{J} 2000.0}$ | $V_{\mathrm{mag}}$ |
| :--- | :--- | :---: | :---: | :---: |
| Variable | NO Cam | $04^{\mathrm{h}} 14^{\mathrm{m}} 51^{\mathrm{s} .4}$ | $+75^{\circ} 20^{\prime} 40^{\prime \prime} 7$ | 12.28 |
| Comparison | UCAC4 $827-007726$ | $04^{\mathrm{h}} 15^{\mathrm{m}} 56^{\mathrm{s} .4}$ | $+75^{\circ} 21^{\prime} 40^{\prime \prime} 1$ | 12.55 |
| Check | UCAC4 $827-007718$ | $04^{\mathrm{h}} 15^{\mathrm{m}} 45^{\mathrm{s} .1}$ | $+75^{\circ} 17^{\prime} 14^{\prime \prime} 6$ | 12.38 |

hotter one, while the less massive component is the hotter one in W-subtype systems.

Furthermore, more and more binaries are found in triple or multiple systems (Liao \& Qian 2010) and several binaries with close-in companions have been reported recently (Qian et al. 2015), which makes the formation and evolutionary process of W UMa-type binaries more complex. Therefore, detailed light curve and orbital period analysis of W UMatype binaries are still needed, which will provide invaluable information for the formation and evolutionary scenario of overcontact binaries.

NO Cam ( $=$ NSV 1495, $V=12.28$ ) is a newly discovered variable star observed by the ROTSE All-Sky Survey I (Akerlof et al. 2000). It was listed as NSV 1495 in the NSV Catalogue (Blattler \& Diethelm 2006), pointing out that it was a W UMa-type overcontact binary with spectral type F5. Since then, several times of minimum light have been published (e.g., Blattler \& Diethelm 2006; Diethelm 2009; Nelson 2010). However, there is currently no spectroscopic element, photometric solution, or period research. In the present paper, $V-, R_{C^{-}}$, and $I_{C^{-}}$band light curves are analyzed using the Wilson-Devinney program and reliable photometric parameters are obtained. All times of minimum light are collected and the period variations are determined. The dynamic interaction and evolutionary scenario are discussed to understand the nature of W UMa-type binaries.

## 2 Multi-color CCD photometric observations

Multi-color light curve observations were carried out on 2013 January 13 and March 15 using the 85 cm reflecting telescope at Xinglong Observation Base, National Astronomical Observatories, Chinese Academy of Sciences. The telescope is located about 960 m above sea level. An Andor DW436 1K CCD camera is attached to the telescope. The effective field of view is 16.5 by 16.5 , corresponding to a plate scale of $0.97 \mathrm{arcsec}^{\text {pixel }}{ }^{-1}$ (Zhou et al. 2009). The operating temperature of the CCD camera was set to be $-55^{\circ} \mathrm{C}$. The broadband Johnson-Cousins $V, R_{\mathrm{C}}, I_{\mathrm{C}}$ filters were used during the observations. UCAC4 827-007726 and UCAC4 827-007718 were chosen as the comparison star (C) and the check star (Ch), respectively. Their coordinates and $V$-band magnitudes are listed in table 1 ; the finding chart is shown in figure 1 . The same integration


Fig. 1. Finding chart. (Color online)
time for the observations on January 13 and March 15 was used: 30 s for $V$ band, 20 s for $R_{\mathrm{C}}$ band, and 15 s for $I_{\mathrm{C}}$ band. Since the comparison and check stars are very close to the target, the extinction differences were negligible. The PHOT package in IRAF $^{1}$ was used to process the observational images. The average observational errors were $0.003 \mathrm{mag}(V), 0.002 \mathrm{mag}\left(R_{\mathrm{C}}\right)$, and $0.002 \mathrm{mag}\left(I_{\mathrm{C}}\right)$. A differential aperture photometry method is applied to determine the light variations. The light curves are displayed in figure 2 and a few lines of the observational data are shown in table 2. The standard deviations of the C and Ch data are all 0.008 mag for the $V, R_{\mathrm{C}}, I_{\mathrm{C}}$ bands. The observational HJD are converted to phase with the following linear ephemeris:
$\operatorname{Min} . \mathrm{I}(\mathrm{HJD})=2456306.2287+0 \mathrm{~d} .430754 \times E$.

Six CCD times of minimum light were determined, and the averaged values are listed in table 3.

[^0]Table 2. Observational data.*

| HJD <br> $2456300+$ | Phase | $\Delta m$ | HJD <br> $2456300+$ |  | Phase | $\Delta m$ | HJD <br> $2456300+$ | Phase |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

*These are only a few lines of the observational data; the entire dataset is available as "Supporting Information" in the online version of this paper.


Fig. 2. Observed light curves. Open circles and crosses refer to data observed on January 13 and March 15, respectively.

## 3 Orbital period investigation

The $\mathrm{O}-\mathrm{C}$ method is the traditional way to reveal variations of orbital period. In the present work, a total of 16 CCD times of minimum light are collected, as listed in table 4 , where " $p$ " refers to the primary minimum and " $s$ " refers to the secondary minimum. The initial residuals (Residuals ${ }_{1}$ ) from equation (2) are listed in the fourth column of table 4:
$\operatorname{Min} . I(H J D)=2455480.8973+0.430754 \times E$.

When a quadratic curve is applied to the initial residuals, Residuals $_{2}$ are obtained and a periodic variation appears, as displayed in the middle of figure 3. Therefore, a sinusoidal term is superimposed on the ephemeris. Based on the least-squares method with the data weighted equally,

Table 3. New CCD times of minimum light.

| JD (Hel.) | Error (d) | Min. | Filter | Telescope* $^{*}$ |
| :---: | :---: | :---: | :---: | :---: |
| 2456228.2601 | $\pm 0.0008$ | I | $B V R_{\mathrm{C}} I_{\mathrm{C}}$ | 60 cm |
| 2456301.2753 | $\pm 0.0003$ | II | $V R_{\mathrm{C}} I_{\mathrm{C}}$ | 85 cm |
| 2456306.0135 | $\pm 0.0001$ | II | $V R_{\mathrm{C}} I_{\mathrm{C}}$ | 85 cm |
| 2456306.2287 | $\pm 0.0001$ | I | $V R_{\mathrm{C}} I_{\mathrm{C}}$ | 85 cm |
| 2456351.0276 | $\pm 0.0001$ | I | $V R_{\mathrm{C}} I_{\mathrm{C}}$ | 85 cm |
| 2456630.1596 | $\pm 0.0001$ | I | $I_{\mathrm{C}} N$ | 1 m |

* 60 cm and 1 m denote the 60 cm and 1 m reflecting telescope at Yunnan Observatories; 85 cm denotes the 85 cm reflecting telescope at Xinglong Observation base.
the revised ephemeris is
Min. $I=2455480.8975( \pm 0.0001)$

$$
\begin{align*}
& +0.43075666( \pm 0.00000006) \times E \\
& +3.15( \pm 0.08) \times 10^{-10} \times E^{2} \\
& +0.00153( \pm 0.00015) \sin [0.191( \pm 0.001) \\
& \times E-20.9( \pm 4.2)] \tag{3}
\end{align*}
$$

We conclude that the period is increasing continuously, at a rate of $d P / d t=+1.46 \times 10^{-9}$, and the periodic change span is $P_{3}=2.2 \mathrm{yr}$ with an amplitude of $A_{3}=0.00153 \mathrm{~d}$. The results from equation (3) are displayed in figure 3.

Since the first data ( $E=-9247$ ) listed in table 4 is quite far away from the others, we remove it and do another trial. The most probable ephemeris is:

$$
\begin{align*}
\text { Min.I }= & 2455480.8974( \pm 0.0001) \\
& +0.4307565( \pm 0.0000001) \times E \\
& +4.33( \pm 0.58) \times 10^{-10} \times E^{2} \\
& +0.00150( \pm 0.00014) \\
& \times \sin [0.189( \pm 0.001) \times E-17.0( \pm 4.5)] \tag{4}
\end{align*}
$$

Table 4. Times of minimum light.

| JD(Hel.) | p/s | Epoch | Residuals | Error |  |
| :--- | :---: | :---: | :---: | :--- | :--- |
| $(2400000+$ ) |  |  |  | Reference |  |
| 51497.7180 | p | -9247 | 0.00294 |  | Blattler and Diethelm (2006) |
| 54833.6883 | s | -1502.5 | -0.00111 | 0.0004 | Diethelm (2009) |
| 55108.9387 | s | -863.5 | -0.00252 | 0.0001 | Nelson (2010) |
| 55127.8930 | s | -819.5 | -0.0014 | 0.0002 | Diethelm (2010) |
| 55480.8973 | p | 0 | 0 | 0.0002 | Diethelm (2011) |
| 55590.3107 | p | 254 | 0.00188 | 0.0020 | Hubscher (2011) |
| 55590.5256 | s | 254.5 | 0.00141 | 0.0016 | Hubscher (2011) |
| 55592.2489 | s | 258.5 | 0.00169 | 0.0010 | Hubscher (2011) |
| 55599.3562 | p | 275 | 0.00155 | 0.0008 | Hubscher (2011) |
| 55599.5705 | s | 275.5 | 0.00047 | 0.0014 | Hubscher (2011) |
| 55627.3569 | p | 340 | 0.00324 | 0.0047 | Hubscher, Lehmann, and Walter (2012) |
| 55627.5705 | s | 340.5 | 0.00146 | 0.0042 | Hubscher, Lehmann, and Walter (2012) |
| 55670.4308 | p | 440 | 0.00174 | 0.0037 | Hubscher, Lehmann, and Walter (2012) |
| 55863.8420 | p | 889 | 0.00439 | 0.0004 | Hubscher, Lehmann, and Walter (2012) |
| 56228.2601 | p | 1735 | 0.00461 | 0.0008 | The present work |
| 56230.8428 | p | 1741 | 0.00279 | 0.0019 | Diethelm (2013) |
| 56301.2753 | s | 1904.5 | 0.00701 | 0.0003 | The present work |
| 56306.0135 | s | 1915.5 | 0.00691 | 0.0001 | The present work |
| 56306.2287 | p | 1916 | 0.00674 | 0.0001 | The present work |
| 56342.4110 | p | 2000 | 0.0057 | 0.0008 | Hoňková et al. (2013) |
| 56351.0276 | p | 2020 | 0.00722 | 0.0001 | The present work |
| 56630.1596 | p | 2668 | 0.01063 | 0.0001 | The present work |
|  |  |  |  |  |  |



Fig. 3. In the upper panel, the dots represent the initial residuals calculated from equation (2). The solid line is the theoretical curve corresponding to equation (3), which contains an upward parabolic variation and a cyclic change, and the dashed line refers to the quadratic term in the equation. In the middle panel, the quadratic part from equation (3) is subtracted to make the periodic change clearer. The residuals are plotted in the bottom panel when both the upward parabolic change and the cyclic variation are removed.


Fig. 4. $O-C$ curve from equation (4).

The results also determined a continuous period increase $\left(d P / d t=+2.01 \times 10^{-9}\right)$ and a cyclic period change ( $P_{3}=2.25 \mathrm{yr}, A_{3}=0.00150 \mathrm{~d}$ ), as shown in figure 4.

Comparing the results from equation (3) with equation (4), we can conclude that the quadratic term makes little difference, but the periodic parts are almost the same. To check the reliability of the results, more times of minimum light are still needed in the future. We will adopt the results from equation (3) for further discussion in the paper hereafter.

## 4 Photometric solutions

As shown in figure 2, the light curves vary continuously, and the depth of the primary and secondary minima are almost equal, which indicates that NO Cam is a typical W UMatype overcontact binary. To derive its physical parameters, the 2013 version of the Wilson-Devinney program (Wilson \& Devinney 1971; Van Hamme \& Wilson 2007; Wilson et al. 2010) is used. The number of observational data used in the program are 444 in the $V$ band, 445 in the $R_{\mathrm{C}}$ band, and 437 in the $I_{\mathrm{C}}$ band. The observational HJD were converted to phase while applying the program.

The spectral type given in the NSV Catalogue (Blattler \& Diethelm 2006) is F5. The 2MASS All Sky Catalogue (Cutri et al. 2003) gives a color index of $J-H=0.220$, which also corresponds to a spectral type of F5. Thus, the effective surface temperature of the primary star (the star eclipsed at primary minimum) is set to be $T_{1}=6530 \mathrm{~K}$ (Cox 2000). Convective atmospheres are assumed, and the corresponding gravity-darkening coefficients of $g_{1}=g_{2}=0.32$ (Lucy 1967)
and bolometric albedo of $A_{1}=A_{2}=0.5$ (Ruciński 1969) are assigned. The limb-darkening coefficients originate from the table in Van Hamme (1993) by considering a logarithmic law accordingly.

Mode 3 for the contact system is adopted. As it is a total eclipsing binary, the mass ratio will be well-determined from light curves since the amplitude of light variation depends mainly on the mass ratio for total annular eclipsing binaries, whereas the amplitude also depends strongly on inclination (Terrell \& Wilson 2005) for partial eclipses. The adjustable parameters are: mass ratio $q\left(M_{2} / M_{1}\right)$; orbital inclination $i$; effective temperature of the secondary star $T_{2}$; monochromatic luminosity of the primary star $L_{1 V}, L_{1 R}$, and $L_{11}$; the dimensionless potential of the primary and secondary stars ( $\Omega_{1}=\Omega_{2}$ in this case); and the third light $l_{3}$. In our solutions, we find that the contribution of third light is negligible. The converged photometric solutions are listed in table 5, Solutions A. The theoretical light curves are displayed in figure 5 . The standard deviations of the fitting residuals are $0.009 \mathrm{mag}(V), 0.007 \mathrm{mag}\left(R_{\mathrm{C}}\right)$, and $0.007 \mathrm{mag}\left(I_{\mathrm{C}}\right)$.

Since the light curves show very good symmetry and Solutions A for convective parameters imply that there may be no spot on the stars, radiative parameters of $g_{1}=g_{2}=1.00$ (Lucy 1967) and $A_{1}=A_{2}=1.00$ (Ruciński 1969) are tried, and Solutions B is obtained in table 5. The theoretical light curves for Solutions B is almost the same as those in figure 5, so they are not displayed here. Comparing Solutions A with Solutions B, it is found that the convective parameters determine a smaller temperature difference and residual, which may be much more

Table 5. Photometric solutions.

| Parameters | Solutions A | Solutions B |
| :--- | :---: | :---: |
| $T_{1}(K)$ | 6530 (fixed) | 6530 (fixed) |
| $g_{1}$ | 0.32 (fixed) | 1.00 (fixed) |
| $g_{2}$ | 0.32 (fixed) | 1.00 (fixed) |
| $A_{1}$ | 0.50 (fixed) | 1.00 (fixed) |
| $A_{2}$ | 0.50 (fixed) | 1.00 (fixed) |
| $a\left(R_{\odot}\right)$ | $3.03($ fixed | $3.02($ fixed $)$ |
| $\mathrm{q}\left(M_{2} / M_{1}\right)$ | $0.439( \pm 0.001)$ | $0.416( \pm 0.001)$ |
| $i\left({ }^{\circ}\right)$ | $84.5( \pm 0.1)$ | $83.8( \pm 0.1)$ |
| $\Omega_{1}=\Omega_{2}$ | $2.6099( \pm 0.0036)$ | $2.6097( \pm 0.0036)$ |
| $T_{2}(\mathrm{~K})$ | $6486( \pm 3)$ | $6304( \pm 4)$ |
| $\Delta T(\mathrm{~K})$ | 44 | 226 |
| $T_{2} / T_{1}$ | $0.9933( \pm 0.0005)$ | $0.9654( \pm 0.0006)$ |
| $L_{1} /\left(L_{1}+L_{2}\right)(V)$ | $0.6731( \pm 0.0002)$ | $0.7141( \pm 0.0003)$ |
| $L_{1} /\left(L_{1}+L_{2}\right)\left(R_{\mathrm{C}}\right)$ | $0.6721( \pm 0.0003)$ | $0.7094( \pm 0.0003)$ |
| $L_{1} /\left(L_{1}+L_{2}\right)\left(I_{\mathrm{C}}\right)$ | $0.6713( \pm 0.0003)$ | $0.7052( \pm 0.0003)$ |
| $r_{1}($ pole $)$ | $0.4527( \pm 0.0005)$ | $0.4483( \pm 0.0005)$ |
| $r_{1}($ side $)$ | $0.4896( \pm 0.0006)$ | $0.4830( \pm 0.0006)$ |
| $r_{1}($ back $)$ | $0.5298( \pm 0.0008)$ | $0.5179( \pm 0.0007)$ |
| $r_{2}($ pole $)$ | $0.3189( \pm 0.0015)$ | $0.3053( \pm 0.0014)$ |
| $r_{2}($ side $)$ | $0.3378( \pm 0.0019)$ | $0.3216( \pm 0.0018)$ |
| $r_{2}($ back $)$ | $0.3986( \pm 0.0044)$ | $0.3713( \pm 0.0036)$ |
| $f$ | $55.5 \%( \pm 1.4 \%)$ | $39.6 \%( \pm 1.4 \%)$ |
| $\Sigma \omega(\mathrm{O}-C)^{2}$ | 0.005229 | 0.005288 |



Fig. 5. Light curve comparison: Open circles refer to observed light curves and red lines correspond to theoretical light curves. (Color online)
acceptable. Solutions A will be used for further discussion hereafter.

## 5 Discussions and conclusions

The light curve solutions suggest that NO Cam is an A-subtype overcontact binary with a mass ratio of $q=0.439$. The contact degree of $f=55.5 \%$ reveals that it is a deep contact system (Qian et al. 2005). The two components have nearly the same surface temperature ( $\Delta T=44 \mathrm{~K}$ )
in spite of their quite different masses and radii, which indicates that the system is under thermal contact. The primary component contributes about $67 \%$ of the total luminosity, and the existence of the third light $\left(l_{3}\right)$ is not detected. The orbital inclination is $i=84.5$, which confirms our assumption that NO Cam is a totally eclipsing binary, indicating that the photometric parameters are derived reliably. As there are no radial velocity curves, we cannot give a direct determination of the absolute parameters. Assuming that the primary component is a normal main-sequence star, its mass is estimated to be $M_{1}=1.4 M_{\odot}(\operatorname{Cox} 2000)$. Considering the mass ratio obtained, the mass of the secondary star is calculated to be $M_{2}=0.61 M_{\odot}$. The semi-major axis listed in table 5 is calculated according to the assumed masses. According to the statistical analysis conducted by Yang and Qian (2015), F-type contact binaries have a really high ratio in extreme mass ratio, overcontact binary systems. It is supposed that NO Cam may evolve into an extreme mass ratio, overcontact binary system and merge into a single rapidly rotating star as in the case of V1309 Sco (Nandez et al. 2014; Zhu et al. 2016).

The period analysis shows that its orbital period is increasing at a rate of $d P / d t=+1.46 \times 10^{-9}$. To account for the period increase, a conservative mass transfer mechanism is supposed. Applying the estimated masses to the well-known equation
$\frac{d M_{2}}{d t}=-\frac{M_{1} M_{2}}{3 P\left(M_{1}-M_{2}\right)} \times d P / d t$,
we conclude that the period increase is due to mass transfer from the less massive component to the more massive one. The mass transfer rate is $\frac{d M_{2}}{d t}=8.37 \times 10^{-8} M_{\odot} \mathrm{yr}^{-1}$. However, the real mass transfer rate may be quite different from this value when the contribution of angular momentum loss is considered.

As shown in the middle panel of figure 3, there may be a cyclic variation superimposed on the period variations. Cyclic oscillations are usually encountered for W UMatype overcontact binary stars (Qian 2003), which could be plausibly explained as the light-travel-time effect arising from the gravitational influence of a third object (Liao \& Qian 2010). By assuming a circular orbit, the projected orbital radius rotating around the barycenter of the triple system is calculated with the equation
$a_{12}^{\prime} \sin i^{\prime}=A_{3} \times c$,
where $A_{3}$ is the amplitude of periodic variation and $c$ is the speed of light. Therefore, the projected orbital radius is calculated to be $a_{12}^{\prime} \sin i^{\prime}=0.26( \pm 0.02)$ au. Considering the mass function of the triple system and the masses of the


Fig. 6. Left panel: Relation between the mass $M_{3}$ (in units of $M_{\odot}$ ) of the third component and its orbital inclination $i^{\prime}\left({ }^{\circ}\right)$. Right panel: Relations between the orbital radius $a_{3}$ (in units of au ) of the third component and its orbital inclination $i^{\prime}\left({ }^{\circ}\right)$. The red star is the position of the tertiary component when it is coplanar with NO Cam. (Color online)
primary and secondary stars, the mass and orbital radius of the tertiary companion are computed with the equation
$f(m)=\frac{4 \pi^{2}}{G P_{3}^{2}} \times\left(a_{12}^{\prime} \sin i^{\prime}\right)^{3}=\frac{\left(M_{3} \sin i^{\prime}\right)^{3}}{\left(M_{1}+M_{2}+M_{3}\right)^{2}}$,
where $G$ is the gravitational constant and $P_{3}$ is the period that the tertiary component orbits around NO Cam. The mass function is calculated to be $f(m)=0.00373 M_{\odot}$. The $i^{\prime}-M_{3}$ and $i^{\prime}-a_{3}$ diagrams are shown in figure 6 , where the red stars are the mass and orbital radius of the tertiary component when the three components are coplanar.

Although tertiary components are quite common in W UMa systems, their effects on the hosting binaries are not clear. They supposedly accelerate the orbital evolution of the hosting binary by removing angular momentum from it during the early dynamical interaction (Qian et al. 2013, 2014b). According to our calculation, NO Cam is a triple system with a cool stellar companion at an orbital separation of about 1.95 au . Recently, some binaries with close-in companions have been reported, as listed in table 6. It should be mentioned that the masses are minimum values since we do not know the orbital inclination $\left(i^{\prime}\right)$ of the tertiary components. The most special one is CSTAR 038663, in which the tertiary component is only about 1 au from the central binary system. Dynamic interaction among the triple system must have a significant influence on the formation of the binary system. Contact binaries with close-in

Table 6. Parameters of close-in companions to contact binaries ( $i^{\prime}=90^{\circ}$ ).

| Target | $M_{3}$ <br> $\left(M_{\odot}\right)$ | $a_{3}$ <br> $(\mathrm{au})$ | Reference |
| :--- | :---: | :--- | :---: |
| PY Vir | 0.79 | 2.8 | Zhu et al. (2013a) |
| V401 Cyg | 0.70 | 2.4 | Zhu et al. (2013b) |
| CSTAR 038663 | 0.63 | 0.93 | Qian et al. (2014a) |
| SDSS J001641-000925 | 0.14 | 2.8 | Qian et al. (2015) |
| V384 Ser | 0.37 | 2.0 | Liao et al. (2015) |
| NO Cam | 0.27 | 1.96 | The present work |

companions are important targets for testing theories of star formation and interaction, and should be studied over the long term.

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## Supporting information

Supplementary data are available at PASJ online.
Complete dataset of table 2.

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[^0]:    ${ }^{1}$ The Image Reduction and Analysis Facility is hosted by the National Optical Astronomy Observatories in Tucson, Arizona at 〈http://iraf.noao.edu〉.

